



اختبار تجريبي

تفاعل وتكامل (باللغة الانجليزية) الصف الثالث الثانوي



1) If  $f(x) = x^3 - 3x - 1$ , then the function has a local minimum value at the point .....

- (A) (-1, 1)
- (B) (-1, 3)
- (C) (1, -3)
- (D) (1, -1)

2)  $\int e^{\cot x} \csc^2 x \, dx = \dots\dots\dots + c$  where c is constant

- (A)  $-e^{\cot x}$
- (B)  $e^{\cot x}$
- (C)  $-e^{\tan x}$
- (D)  $e^{\tan x}$

3)  $\int \ln \sqrt{x} \, dx = \dots\dots\dots + c$  where c is constant

- (A)  $\frac{1}{2} x \ln \frac{e}{x}$
- (B)  $\frac{1}{2} x \frac{\log x}{\log e}$
- (C)  $\frac{1}{2} x \frac{\log e}{\log x}$
- (D)  $\frac{1}{2} x \ln \frac{x}{e}$



4) The slope of the tangent to the curve  $y = \tan \theta$ ,  $x = \cot \theta$  at the point  $(2, \frac{1}{2})$  equals.....

- (A) 4
- (B)  $-\frac{1}{4}$
- (C) -4
- (D)  $\frac{1}{4}$

5) If  $\lim_{x \rightarrow 0} \frac{e^{2x} + \tan ax - 1}{x} = 1$ , then  $a = \dots\dots\dots$

- (A) -2
- (B) 1
- (C) -1
- (D) 2

6) If  $y = f(x)$  is a function its curve passing through the origin where  $\frac{dx}{dy} = \frac{1}{2x+1}$  for all points of the curve, then  $y = \dots\dots\dots$

- (A)  $x^2 + 2x$
- (B)  $x^2 + x$
- (C)  $\frac{1}{2}x^2 + x$
- (D)  $x^2 + \frac{1}{2}x$



7) The area of the region bounded by the curve  $y = x^2 - 9$  and the straight line  $x = 4$  above  $x$ -axis equals..... units of area

- (A)  $\frac{20}{3}$
- (B)  $\frac{47}{3}$
- (C)  $\frac{5}{3}$
- (D)  $\frac{10}{3}$

8)  $\int \frac{\cos 2x}{(\sin x - \cos x)^2} dx = \dots\dots\dots + c$  where  $c$  is constant

- (A)  $\ln |\cos x - \sin x|$
- (B)  $-\ln |\cos x + \sin x|$
- (C)  $-\ln |\cos x - \sin x|$
- (D)  $\ln |\cos x + \sin x|$

9) If  $x \log_y e = 1$ , then  $\frac{dy}{dx} = \dots\dots\dots$  at  $x = 1$

- (A)  $e$
- (B)  $1$
- (C)  $\frac{1}{e}$
- (D)  $-e$



10) The equation of the tangent to the curve  $y = e^x$  at the point  $(1, e)$  is.....

(A)  $ey + x = 0$

(B)  $y - ex = 0$

(C)  $ey - x = 0$

(D)  $y + ex = 0$

11) If  $0 < a < b < \frac{\pi}{2}$ , then  $\int_a^b \tan^2 x \, dx + \int_b^a \sec^2 x \, dx = \dots\dots\dots$

(A)  $b - a$

(B)  $-1$

(C)  $1$

(D)  $a - b$

12) The volume of the solid generated by revolving the region bounded by the curve of the function  $y = x^2$  and the straight line  $y = x + 2$  a complete revolution about  $x$  - axis equals..... units of volume

(A)  $\frac{81}{10} \pi$

(B)  $\frac{72}{5} \pi$

(C)  $\frac{92}{15} \pi$

(D)  $\frac{7}{6} \pi$



اختبار تجريبي

تفاعل وتكامل (باللغة الانجليزية) الصف الثالث الثانوي



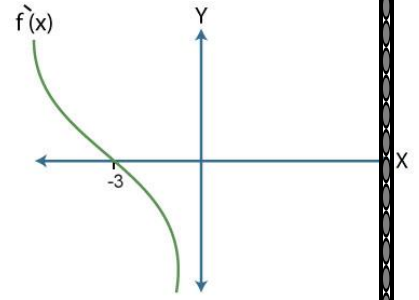
13) If  $y = x \ln x - 3x$ , then the minimum value of  $x + y$  is .....

- (A) -e
- (B) -2e
- (C) -e<sup>2</sup>
- (D) -2

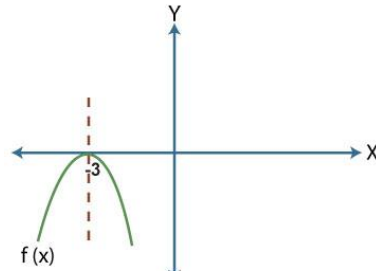
14) If  $xy - 8 \log e = 0$ , then  $\frac{d^2y}{dx^2} = \dots\dots\dots$

- (A)  $\frac{-x}{y^2}$
- (B)  $\frac{2x}{y^2}$
- (C)  $\frac{-y}{x^2}$
- (D)  $\frac{2y}{x^2}$

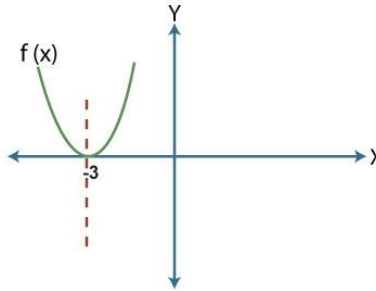
15) If  $f'(x)$  is represented by the given figure, then  $f(x)$  is represented by the figure



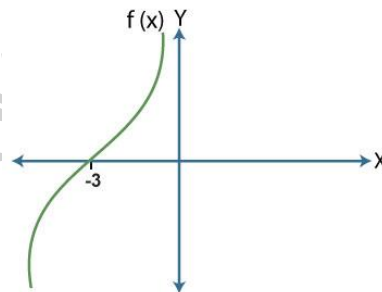
(A)



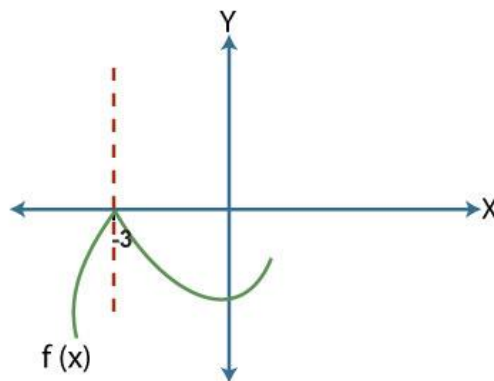
(B)



(C)



(D)





16) The curve of the function  $y = x e^{x+k}$  has a point of inflection at  $x = \dots$  where  $k$  is constant

- (A)  $k$
- (B)  $2$
- (C)  $-2$
- (D)  $-k$

17) If  $x = x^{\sec y} - 2$ , then  $\frac{8}{\sqrt{3}} \frac{dy}{dx} = \dots$  at the point  $(2, \frac{\pi}{3})$

- (A)  $-\log_2 e$
- (B)  $\log_2 e$
- (C)  $-\ln 2$
- (D)  $\ln 2$

18) If the rate of change of the lateral area of a cube at a given moment numerically equals the rate of change of its edge length, then the length of the edge of this cube equals.....length units at this moment.

- (A)  $\frac{1}{16}$
- (B)  $\frac{1}{8}$
- (C)  $\frac{1}{4}$
- (D)  $\frac{1}{2}$

19) If  $f(x) = ax - x^3$  where  $x \in [0, 4]$  and  $f(1)$  is the absolute maximum value of the function, then find its absolute minimum value of the function where  $a$  is constant.

20) The given figure represents the curve  $y^2 = 4x$  where  $y \geq 0$ , and the two straight lines  $x = 2y$ ,  $x + y = 3$

Find the area of the shaded region.

